Clinical Pharmacokinetics

Clinical Pharmacokinetic Equations and Calculations

One-compartment model equations for linear pharmacokinetics

1. Intravenous Bolus Equation

• When a drug is given as an intravenous bolus and the drug distributes from the blood into the tissues quickly, the serum concentrations often decline in a straight line when plotted on semilogarithmic axes.

$$C = (D/V)e^{-k_e t}$$

 Most drugs given intravenously cannot be given as an actual intravenous bolus because of side effects related to rapid injection. A short infusion of 5– 30 minutes can avoid these types of adverse effects, and if the intravenous infusion time is very short compared to the half-life of the drug so that a large amount of drug is not eliminated during the infusion time, intravenous bolus equations can still be used.



• Pharmacokinetic parameters for patients can also be computed for use in the equations. If two or more serum concentrations are obtained after an intravenous bolus dose, the *elimination rate constant*, *half-life* and *volume of distribution* can be calculated.

$$k_e = 0.693/t_{1/2}$$

• The elimination rate constant can be computed using the following equation:

$$k_e = -(\ln C_1 - \ln C_2)/(t_1 - t_2)$$

1

where t1 and C1 are the first time/concentration pair and t2 and C2 are the second time/concentration pair

Clinical Pharmacokinetics

• The volume of distribution can be calculated by dividing the dose by the serum concentration at time = 0.

$$V = D/C_0$$

2. Continuous and Intermittent Intravenous Infusion Equations

- Some drugs are administered using a continuous intravenous infusion, and if the infusion is discontinued the serum concentration/time profile decreases in a straight line when graphed on a semilogarithmic axes.
- one compartment model intravenous infusion equation can be used to compute concentrations (C) while the infusion is running:

$$C = (k_0/Cl)(1 - e^{-k_e t}) = [k_0/(k_e V)](1 - e^{-k_e t})$$

where k_0 is the drug infusion rate (in amount per unit time, such as mg/h or µg/min), Cl is the drug clearance (since $Cl = k_eV$, this substitution was made in the second version of the equation), k_e is the elimination rate constant, and t is the time that the infusion has been running.

• If the infusion is allowed to continue until steady state is achieved, the steady-state concentration (Css) can be calculated easily:

$$Css = k_0/Cl = k_0/(k_eV)$$

• If the infusion is stopped, postinfusion serum concentrations ($C_{postinfusion}$) can be computed by calculating the concentration when the infusion ended (C_{end}) using the appropriate equation in the preceding paragraph, and the following equation:

$$C_{\text{postinfusion}} = C_{\text{end}} e^{-k_e t_{\text{postinfusion}}}$$

 $t_{postinfusion}$ is the postinfusion time ($t_{postinfusion} = 0$ at end of infusion and increases from that point).

• Pharmacokinetic parameters for patients can also be computed for use in the equations. If two or more serum concentrations are obtained after an intravenous bolus dose, the *elimination rate constant*, *half-life* and *volume of distribution* can be calculated.

$$k_e = 0.693/t_{1/2}$$

• The elimination rate constant can be computed using the following equation:

$$k_{e} = -(\ln C_{1} - \ln C_{2})/(t_{1} - t_{2})$$

where t1 and C1 are the first time/concentration pair and t2 and C2 are the second time/concentration pair

Clinical Pharmacokinetics

• The volume of distribution (V) can be computed using the following equation:

$$V = \frac{k_0 (1 - e^{-k_e t'})}{k_e [C_{max} - (C_{predose} e^{-k_e t'})]}$$

where k_0 is the infusion rate, ke is the elimination rate constant, t' = infusion time, Cmax is the maximum concentration at the end of infusion, and Cpredose is the predose concentration.



FIGURE 2-5 If a drug is given as a continuous intravenous infusion, serum concentrations increase until a steady-state concentration (*Css*) is achieved in 5–7 half-lives. The steady-state concentration is determined by the quotient of the infusion rate (k_0) and drug clearance (*Cl*): Css = k_0 /Cl. When the infusion is discontinued, serum concentrations decline in a straight line if the graph is plotted on semilogarithmic axes. When using \log_{10} graph paper, the elimination rate constant (k_e) can be computed using the following formula: slope = $-k_e/2.303$.