

Introduction:	
 Linear pharmacokinetics: When the dose of a drug is increased, we expect that the concentration at steady state(Css) will increase proportionately, i.e. if the dose rate is increased or decreased say two-fold, the plasma drug concentration will also increase or decrease two-fold. Nonlinear pharmacokinetics the plasma drug concentration changes either more or less than would be expected from a change in dose rate. This can cause problems when adjusting doses. This is because one or more of the kinetic processes (absorption, distribution and/or elimination) of the drug may be occurring via a mechanism other than simple first-order kinetics 	كلية الصيدلة College of Pharmacy

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Linear pharmacokinetics

- Change in plasma concentration due to ADME process is proportional to dose of drug administered (single or multiple)
- Follow First order kinetics
- Semilog plot for concentration vs time is super imposable (Principle of superimposition).
- No change in F, Ka, Ke, Vd, Clearance etc., when different doses are administered and/or when the drug is administered via different routes as a single dose or multiple doses.

Nonlinear Pharmacokinetics

- Saturated process:
 - Rate process of ADME are dependent on carrier or enzymes having definite capacity and subjected to saturation.
- Change in concentration is no more proportional to dose administered during the total process of ADME.
- Follow First order + Zero order kinetics
- Change in different pharmacokinetic parameters depending on the administered dose



The term linear simply means that plasma concentration at a given time at steady state and the area under the plasma concentration versus time curve (AUC) will both be directly proportional to the dose administered





DETECTION OF NONLINEARITY

- Two simple tests for detection of nonlinearity:
- 1. Determination of steady state plasma conc. at different doses.
- 2. Determination of some of the important pharmacokinetic parameters such as fraction bioavailable, elimination half life, or total systemic clearance at different doses of the drug.



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CAUSES OF NONLINEARITY

• one or more of the below kinetic processes of the drug may be occurring via a mechanism other than simple first-order kinetics

➢Drug absorption

- Drug distribution
- Drug metabolism
- Drug excretion

GIT ABSORPTION

- Sources of nonlinearity:
- When absorption is solubility or dissolution rate limited.
 Ex:- Griseofulvin .
- Intestinal metabolism (1st pass metabolism).
 Ex:- Salicylamide , propranolol
- Drugs with low solubility in GI but relatively high dose > Ex:- Chorothiazide , griseofulvin , danazol
- Saturable gastric or GI decomposition
 - Ex:- Penicillin G, omeprazole , saquinavir
- Saturable transport in gut wall
 - \succ Ex:- Riboflavin, gebapentin , L-dopa, baclofen , ceftibuten
- Other causes include change in gastric emptying, GI blood flow & other physiological factors

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•	Sources of nonlinearity in drug distribution:
	Saturation of binding sites on plasma proteins.
>	Saturation of tissue binding sites. ➢ Ex:- thiopental & Fentanyl ., disopyramide
>(Cellular uptake ≻Ex:- Methicillin
	Tissue binding → Ex:- Imiprimine
	CSF transport Ex:- Benzylpenicillins
>	Saturable transport into or out of tissues

DRUG METABOLISM

Causes of nonlinearity in metabolism are:

Capacity limited metabolism due to enzyme & cofactor saturation.

Ex:- Phenytoin, alcohol, theophylline.

- ➤Enzyme induction.
 - Ex:- Carbamazepine, where a decrease in peak plasma concentration has been observed on repetitive administration.
- Cofactor or enzyme limitation

► Ex:- Acetaminophen,

Altered hepatic blood flow

≻Ex:- Propranolol , verapamil Metabolite inhibition Diazepam.

Other causes, saturation of binding sites & pathological situation such as hepatotoxicity

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DRUG EXCRETION

- saturable processes are:
- 1. Active tubular secretion.
 - Ex:- Penicillin G.
- 2. Active tubular reabsorption .
 - Ex:- Water soluble vitamins & glucose.
- 3. Biliary secretion
 - Ex:- lodipamide,
- 4. Enterohepatic recycling
 - Ex:- Cimetidine , isotretinoin .
- 5. Other causes include:
 - 1. forced diuresis,
 - 2. change in pH, nephrotoxicity & saturation of binding sites.



Kinetic of capacity-limited or saturable processes is best described by Michaelis-menten equation

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Elimination rate =
$$\frac{dC_{\rm p}}{dt} = \frac{V_{\rm max}C_{\rm p}}{K_{\rm M} + C_{\rm p}}$$
 (9.1)

Where: V_{max} is the maximum elimination rate K_{M} is the Michaelis constant

- K_M reflects the *capacity* of the enzyme system.
- It is important to note that K_M is not an elimination constant, but is actually a hybrid rate constant in enzyme kinetics, representing both the forward and backward reaction rates and equal to the drug concentration or amount of drug in the body at 0.5V_{max}.
- The values for K_M and V_{max} are dependent on the nature of the drug and the enzymatic process involved.



Example:

The elimination rate of drug X with a K_M of 0.1 ug/mL and a V max of 0.5 ug/mL per hour is calculated by using equation :

Elimination rate =
$$\frac{dC_{\rm p}}{dt} = \frac{V_{\rm max}C_{\rm p}}{K_{\rm M} + C_{\rm p}}$$
 (9.1)

- Rate constant (The ratio of the elimination rate/ the concentration) is not equal at different concentrations.
- In contrast, a first-order elimination process would yield the same elimination rate constant at all plasma drug concentrations.

At drug concentrations of 0.4–10 ug/mL, the enzyme system is not saturated and the rate of elimination is a mixed or nonlinear process

- At higher drug concentrations, 11.2ug/mL and above, the elimination rate approaches the maximum velocity (V max) of approximately 0.5 ug/mL per hour.
- At V max, the elimination rate is a constant and is considered a zero-order process.

)rug Concentration (µg/mL)	Elimination Rate (µg/mL per hr)	Elimination Rate/Concentration ^b (hr ⁻¹) Elimination constant
0.4	0.400	1.000
D.8	0.444	0.556
1.2	0.462	0.385
1.6	0.472	0.294
2.0	0.476	0.238
2.4	0.480	0.200
2.8	0.483	0.172
3.2	0.485	0.152
10.0	0.495	0.0495
10.4	0.495	0.0476
10.8	0.495	0.0459
11.2	0.496	0.0442
11.6	0.496	0.0427

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- When the drug concentration C_p is large in relation to K_M ($C_p >> K_m$), saturation of the enzymes occurs and the value for K_M is negligible.
- The rate of elimination proceeds at a fixed or constant rate equal to V max. Thus, elimination of drug becomes a zero-order process:

Elimination rate =
$$\frac{dC_{\rm p}}{dt} = \frac{V_{\rm max}C_{\rm p}}{K_{\rm M} + C_{\rm p}}$$
 (9.1)

$$-\frac{dC_{\rm p}}{dt} = \frac{V_{\rm max}C_{\rm p}}{C_{\rm p}} = V_{\rm max}$$
(9.2)

Example

- drug X (V max = 0.5 ug/mL per hour, K M = 0.1 ug/mL), how long would it take for the plasma drug concentration to decrease from 20 to 12 ug/mL?
- Solution
- Because 12ug/mL >> Km, elimination occurs at a zero-order rate of approximately 0.5 g/mL per hour.

$$-\frac{dC_{\rm p}}{dt} = \frac{V_{\rm max}C_{\rm p}}{C_{\rm p}} = V_{\rm max} \tag{9.2}$$

Time(dt) =dCp/Vmax \rightarrow time=20-12/0.5g/ml=16hrs

- when drug concentrations are much less than enzyme concentrations. (K_M>>Cp) rate of drug elimination becomes a first-order process.
- enzymatic drug elimination can change from a nonlinear to a linear process over a restricted concentration range.

		Elimination Rate	
Drug Concentration (C _p) (µg/mL)	Elimination Rate (µg/mL per hr)	Concentration (hr ⁻¹) ^b	
0.01	0.011	1.1	1000
0.02	0.022	1.1	
0.03	0.033	1.1	
0.04	0.043	1.1	
0.05	0.053	1.1	
0.06	0.063	1.0	
0.07	0.072	1.0	
0.08	0.082	1.0	N
0.09	0.091	1.0	
This is evident be	cause the rate cor	nstant (or	
elimination rate/d are constant. (Cp ratio of eliminatio	bellow 0.05 ug/r n rate/drug	n) values mL, the	:0

If KM>>>Cp

 $\frac{dC_{\rm p}}{dt} = k'C_{\rm p}$

The first-order rate constant for a saturable process, k', can be calculated from Equation :

$$k' = \frac{V_{\text{max}}}{K_{\text{M}}}$$

• the t 1/2 due to enzymatic elimination can be calculated:

• t1/2=0.693/k'







• In order to calculate the time for the dose of the drug to decline to a certain amount of drug in the body:

$$t = \frac{1}{V_{\text{max}}} \left(D_0 - D_t + K_{\text{M}} \ln \frac{D_0}{D_t} \right)$$
(9.6)

- the time for a single 400-mg dose given by IV bolus injection to decline to 20 mg was calculated for a drug with a K_M of 38 mg/L and a V_{max} that varied from 200 to 100 mg/hr
- With a V max of 200 mg/hr, the time for the 400mg dose to decline to 20 mg in the body is 2.46 hours,
- when the V_{max} is decreased to 100 mg/hr, the time for the 400-mg dose to decrease to 20 mg is increased to 4.93 hours.
- Thus, there is an inverse relationship between the time for the dose to decline to a certain amount of drug in the body and the V_{max}
 - $\frac{1000}{(0)} \frac{1000}{100} \frac{1000}{100} \frac{V_{max}}{V_{max}} = \frac{1}{100} \frac{V_{max}}{V_{max}} =$

- Example:
- A drug eliminated from the body by capacity-limited pharmacokinetics has a $K_{\rm M}$ of 100 mg/L and a $V_{\rm max}$ of 50 mg/hr. If 400 mg of the drug is given to a patient by IV bolus injection, calculate the time for the drug to be 50% eliminated. If 320 mg of the drug is to be given by IV bolus injection, calculate the time for 50% of the dose to be eliminated. Explain why there is a difference in the time for 50% elimination of a 400-mg dose compared to a 320-mg dose.

$$t = \frac{1}{V_{\text{max}}} \left(D_0 - D_t + K_{\text{M}} \ln \frac{D_0}{D_t} \right)$$
(9.6)

Solution

Use Equation 9.6 to calculate the time for the dose to decline to a given amount of drug in the body. For this problem, D_{t} is equal to 50% of the dose D_{0} . If the dose is 400 mg,

$$t = \frac{1}{50} \left(400 - 200 + 100 \ln \frac{400}{200} \right) = 5.39 \text{ hr}$$

If the dose is 320 mg

$$t = \frac{1}{50} \left(320 - 160 + 100 \ln \frac{320}{160} \right) = 4.59 \,\mathrm{hr}$$

For capacity-limited elimination, the elimination half-life is dose-dependent, because the drug elimination process is partially saturated. Therefore, small changes in the dose will produce large differences in the time for 50% drug elimination. The parameters K M and V max determine when the dose is saturated.



- whereas when K_M is 76 mg/L, the time for the drug dose to decline to 20 mg is 3.03 hours.
- Thus, an increase in K_M (with no change in V max) will increase the time for the drug to be eliminated from the body.





• 2. Using the same drug, calculate the time for 50% elimination of the dose when the doses are 10 and 5 mg. Explain why the times for 50% drug elimination are similar even though the dose is reduced by one-half.

$$t = \frac{1}{V_{\text{max}}} \left(D_0 - D_t + K_{\text{M}} \ln \frac{D_0}{D_t} \right)$$
(9.6)

$$t = \frac{1}{50} \left(10 - 5 + 100 \ln \frac{10}{5} \right) = 1.49 \text{ hr}$$

If the dose is 5 mg,

$$t = \frac{1}{50} \left(5 - 2.5 + 100 \ln \frac{5}{2.5} \right) = 1.44 \text{ hr}$$

Whether the patient is given a 10- or a 5-mg dose by IV bolus injection, the times for the amount of drug to decline 50% are approximately the same. For 10- and 5-mg doses the amount of drug in the body is much less than the K M of 100 mg. Therefore, the amount of drug in the body is well below saturation of the elimination process and the drug declines at a first-order rate.







- An example for the determination of K $_{\rm M}$ and V $_{\rm max}$ is given for the drug phenytoin.
- Phenytoin undergoes capacity-limited kinetics at therapeutic drug concentrations in the body.
- To determine $K_{\rm M}$ and $V_{\rm max}$, two different dose regimens are given at different times, until steady state is reached.
- The steady-state drug concentrations are then measured by assay.
- At steady state, the rate of drug metabolism (v) is assumed to be the same as the rate of drug input R (dose/day).

$$R = \frac{V_{\text{max}}C_{\text{SS}}}{K_{\text{M}} + C_{\text{SS}}} \tag{9.11}$$

where R = dose/day or dosing rate;

 $C_{\rm ss}$ = steady-state plasma drug concentration,

 V_{max} = maximum metabolic rate constant in the body, and K_{M} = Michaelis–Menten constant of the drug in the body.



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$$K_{\rm M} = \frac{300 - 150}{(150/8.6) - (300/25.1)} = 27.3 \, {\rm mg/L}$$

Substitute K M into either of the two simultaneous equations to solve for V max.

$$150 = \frac{V_{\max}(8.6)}{27.3 + 8.6}$$
$$V_{\max} = 626 \text{ mg/day}$$

Determination of $K_{\rm M}$ and $V_{\rm max}$ by Direct Method

• When steady-state concentrations of phenytoin are known at only two dose levels, there is no advantage in using the graphic method. $K_{\rm M}$ and $V_{\rm max}$ may be calculated by solving two simultaneous equations formed by substituting $C_{\rm SS}$ and R (Eq. 9.11) with $C_{\rm 1}$, $R_{\rm 1}$, $C_{\rm 2}$, and $R_{\rm 2}$. The equations contain two unknowns, $K_{\rm M}$ and $V_{\rm max}$, and may be solved easily.

$$R_1 = \frac{V_{\text{max}}C_1}{K_{\text{M}} + C_1}$$
$$R_2 = \frac{V_{\text{max}}C_2}{K_{\text{M}} + C_2}$$

Combining the two equations yields Equation 9.15

$$K_{\rm M} = \frac{R_2 - R_1}{(R_1 / C_1) - (R_2 / C_2)} \tag{9.15}$$

where C_1 is steady-state plasma drug concentration after dose 1, C_2 is steady-state plasma drug concentration after dose 2, R_1 is the first dosing rate, and R_2 is the second dosing rate. To calculate K_{M} and V_{max} , use Equation 9.15 with the values $C_1 = 8.6 \text{ mg/L}$, $C_2 = 25.1 \text{ mg/L}$, $R_1 = 150 \text{ mg/day}$, and $R_2 = 300 \text{ mg/day}$. The results are

Interpretation and importance of K M and V max An understanding of Michaelis–Menten kinetics provides insight into the nonlinear kinetics and helps to avoid dosing a drug at a concentration near enzyme saturation. For example, in phenytoin dosing, since K M occurs at 0.5V max, K M = 27.3 mg/L, the implication is that at a plasma concentration of 27.3 mg/L, enzymes responsible for phenytoin metabolism are eliminating the drug at 50% V max, ie, 0.5 x 626 mg/day or 313 mg/day. Patients with a low K M tend to have greater changes in plasma concentrations during dosing adjustments. Patients with a smaller K M (same V max) will show a greater change in the rate of elimination when plasma drug concentration changes compared to subjects with a higher K M.



• The relationship between elimination half-life and drug concentration is:

$$t_{1/2} = \frac{0.693}{V_{\text{max}}} \left(K_{\text{M}} + C_{\text{p}} \right)$$
(9.16)

- 1. in Nonlinear, the elimination half-life becomes longer, clearance becomes smaller, and the area under the curve becomes disproportionately larger with increasing dose.
- 2. The elimination half-life is dependent on the Michaelis–Menten parameters and concentration.
- **3.** <u>It is not preferable</u> to calculate the elimination half-life of a nonlinear drug because the elimination half-life is not constant.
- **4.** *Clinically*, if the half-life is increasing as plasma concentration increases, and there is no apparent change in metabolic or renal function, then there is a good possibility that the drug may be metabolized by nonlinear kinetics.

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Dependence of Clearance on Dose

- The total body clearance that follows a one-compartment model with Michaelis–Menten elimination kinetics changes with respect to time and plasma drug concentration.
- Within a certain drug concentration range, an average or mean clearance (CI_{av}) may be determined.
- Because the drug follows Michaelis–Menten kinetics, Cl av is dose-dependent.

$$Cl_{\rm av} = \frac{V_{\rm max}}{(D_0/2V_{\rm D}) + K_{\rm M}}$$
 (9.23)

$$Cl = \frac{V_{\rm D} (dC_{\rm p}/dt)}{C_{\rm p}} = \frac{V_{\rm max}}{K_{\rm M} + C_{\rm p}}$$
(9.24)

$$Cl_{\rm T} = \frac{dD_{\rm E}/dt}{C_{\rm p}}$$
(9.25)

Mixed Drug Elimination

- The Drugs are metabolized to several different metabolites by parallel pathways.
- For example, sodium salicylate is metabolized to both a glucuronide and a glycine conjugate (hippurate).
- The rate of formation of the glycine conjugate is limited by the amount of glycine available. Thus, the rate of formation of the glucuronide continues as a first-order process; whereas the rate of conjugation with glycine is capacity limited.
- The equation that describes a drug that is eliminated by both first-order and Michaelis–Menten kinetics after IV bolus injection is given by:

$$-\frac{dC_{\rm p}}{dt} = kC_{\rm p} + \frac{V_{\rm max}'C_{\rm p}}{K_{\rm M} + C_{\rm p}}$$
(9.26)

Where:

k is the first-order rate constant representing the sum of all first-order elimination processes, V'_{max} is simply V_{max} expressed as concentration by dividing by V_{D}



First-Order Absorption and Nonlinear Elimination

The relationship that describes the rate of change in the plasma drug concentration for a drug that is given extravascularly (eg, orally), absorbed by first-order absorption, and eliminated only by nonlinear pharmacokinetics, is given by the following equation. C _{GI} is concentration in the GI tract.

$$\frac{dC_{\rm p}}{dt} = k_{\rm a} C_{\rm GI} e^{-k_{\rm a} t} - \frac{V_{\rm max}' C_{\rm p}}{K_{\rm M} + C_{\rm p}}$$
(9.28)

where k_{a} is the first-order absorption rate constant.

If the drug is eliminated by parallel pathways consisting of both linear and nonlinear pharmacokinetics, Equation 9.28 may be extended to Equation 9.29.

$$\frac{dC_{\rm p}}{dt} = k_{\rm a}C_{\rm GI}e^{-k_{\rm a}t} - \frac{V_{\rm max}C_{\rm p}}{K_{\rm M} + C_{\rm p}} - kC_{\rm p} \qquad (9.29)$$

where *k* is the first-order elimination rate constant.

Bioavailability of Drugs that Follow Nonlinear Pharmacokinetics

- The bioavailability of drugs that follow nonlinear pharmacokinetics is difficult to estimate accurately. EXPLAIN WHY?
- As shown in , each process of drug absorption, distribution, and elimination is potentially saturable. Drugs that follow linear pharmacokinetics follow the principle of superposition (). The assumption in applying the rule of superposition is that each dose of drug superimposes on the previous dose. Consequently, the bioavailability of subsequent doses is predictable and not affected by the previous dose. In the presence of a saturable pathway for drug absorption, distribution, or elimination, drug bioavailability will change within a single dose or with subsequent (multiple) doses.

